

lec 14

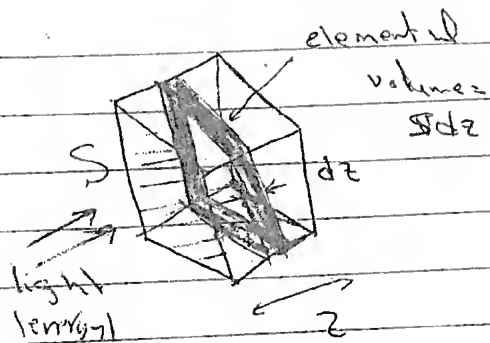
Date: _____

10/11/2018

→ Stimulated Emission Amplification

cross sectional area

propagation direction



energy / unit time

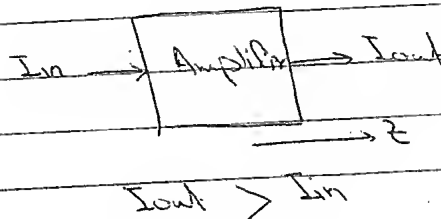
radiance = Power / unit area = I

energy density = energy / unit volume

Absorption (stimulated)

② Stimulated Emission

design amplifier?



coefficient of absorption (B_{ab})

$$R_{ap} = \frac{B}{8\pi h^2 \nu^3} \times P_{\nu} \times P_{abs} \times U$$

where: $B = \frac{u^3}{8\pi h^2 \nu^3}$, $u =$ speed of wave inside material
 $\nu =$ frequency of incident wave

R_{ap} : no. of absorbed photons / unit volume / unit time

$$\text{no. of absorbed photons in volume } (Sdz) = B P_{\nu} \times P_{abs} \times U \times Sdz$$

$$\text{energy absorbed in } Sdz = B P_{\nu} P_{abs} U Sdz \times h\nu$$

Simplify:-

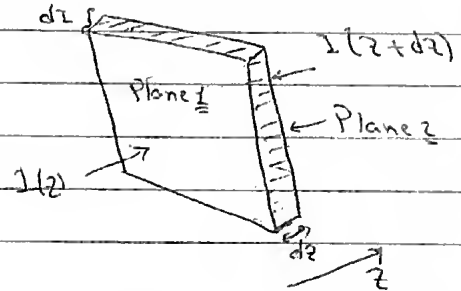
$$\text{Energy emitted} = J_{st} \times S dz \times h\nu$$

$$- B P_e P_e U S dz h\nu$$

$$\text{Net energy} = \text{emitted} - \text{Absorption}$$

$$= B P_e U S dz h\nu (P_e - P_{abs})$$

1 unit time



$$dI \times S \Rightarrow \text{power}$$

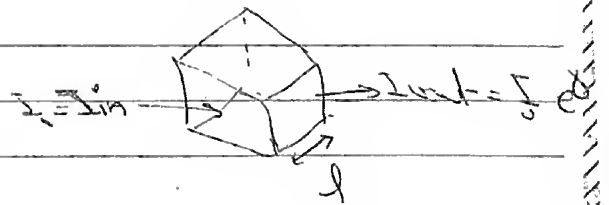
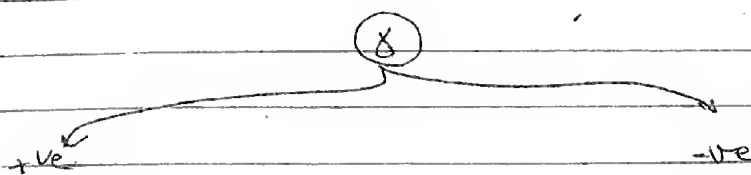
$$dI \times S = B P_e U S dz h\nu (P_e - P_{abs})$$

$$\frac{dI}{dz} = B P_e U h\nu (P_e - P_{abs})$$

$$U = \frac{I}{c}$$

$$\frac{dI}{dz} = \boxed{\frac{B P_e h\nu}{U_{\text{photon}}} (P_e - P_{abs})} I(z)$$

$$\boxed{\frac{dI}{dz} = \gamma I(z)} \quad \therefore I(z) = I_0 e^{\gamma z}$$



$$I_{out} > I_{in}$$

$$I_{out} < I_{in}$$

Amplifier

Attenuator

$$G_{\text{gain}} > 1$$

$$G_{\text{loss}} < 1$$

$$P_e > P_{abs}$$

$$P_e < P_{abs}$$

Date

$$\gamma = \frac{B P_v h \gamma (P_e - P_{abs})}{v}$$

$$P_v = \frac{1}{\pi h^2} (2m)^{3/2} (h\nu - E_g)^{1/2} \rightarrow h\nu > E_g$$

$$B = \frac{v^3}{8\pi h \nu^3}$$

quartz laser diode (Pnp) $\rightarrow P_e > P_{abs} \rightarrow \text{amplifier}$

two Fermi levels E_c, E_v
two Fermi functions.

$$P_e = f_c(E_2) \times [1 - f_v(E_1)] = \frac{1}{e^{(E_2 - E_c)/KT} + 1} \cdot \frac{e^{(E_1 - E_v)/KT}}{e^{(E_1 - E_v)/KT} + 1}$$

$$P_{abs} = f_v(E_1) \times [1 - f_c(E_2)] = \frac{1}{e^{(E_1 - E_v)/KT} + 1} \cdot \frac{e^{(E_2 - E_c)/KT}}{e^{(E_2 - E_c)/KT} + 1}$$

$$P_e > P_{abs}$$

$$e^{(E_1 - E_v)/KT} > \frac{e^{(E_2 - E_c)/KT}}{e^{(E_2 - E_c)/KT} + 1}$$

$$E_1 - E_v > E_2 - E_c$$

$$E_c - E_v > E_2 - E_1$$

$$E_2 - E_1 < E_c - E_v$$

$$h\nu < (E_c - E_v)$$

$$E_g < h\nu < E_c - E_v$$

$$\frac{E_g}{h} < 1 < \frac{E_c - E_v}{h} \rightarrow \text{Amplification}$$

$$P_e - P_{abs} = f_c(E_2) \times [1 - f_v(E_1)] - f_v(E_1) \times [1 - f_c(E_2)]$$

$$= f_c(E_2) - f_v(E_1)$$

$$\delta = \frac{L^3}{8\pi h^2} \times \frac{1}{\pi h^2} (2m)^{3/2} \frac{h\nu}{L} (h\nu - E_g)^{1/2} [f_c(E_2) - f_v(E_1)]$$

$$\delta = \frac{L^2}{2h^2} \frac{(2m)^{3/2}}{L^2} (h\nu - E_g)^{1/2} [f_c(E_2) - f_v(E_1)]$$

ex: at $T = 0^\circ K$

(a) at Thermal equilibrium:

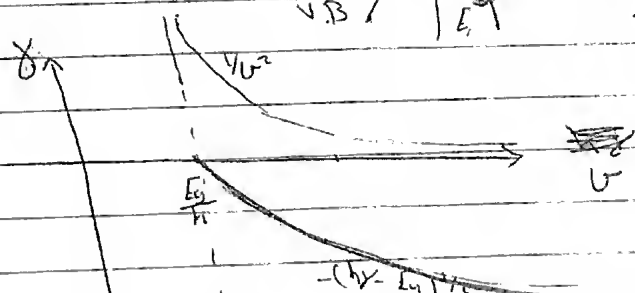
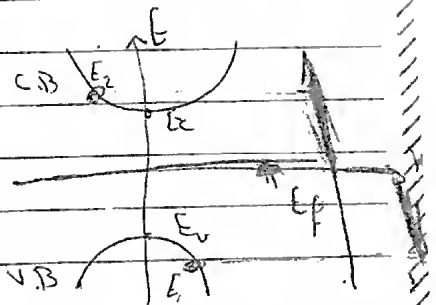
$$f(E_2) = 0$$

$$f(E_1) = 1$$

$$f(E_2) - f(E_1) = -1$$

$$\delta = -ve$$

attenuator



(b) at Quasi Equilibrium:

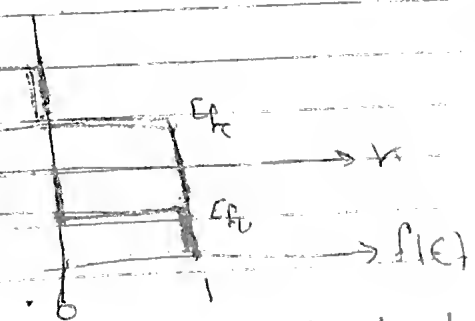
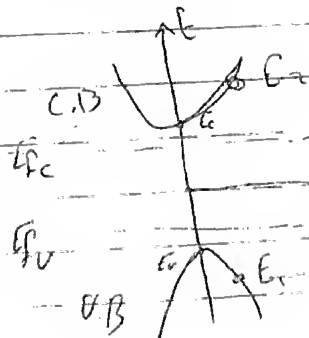
$$f(E_2) = 0$$

$$f(E_1) = 1$$

$$f(E_2) - f(E_1) = -1$$

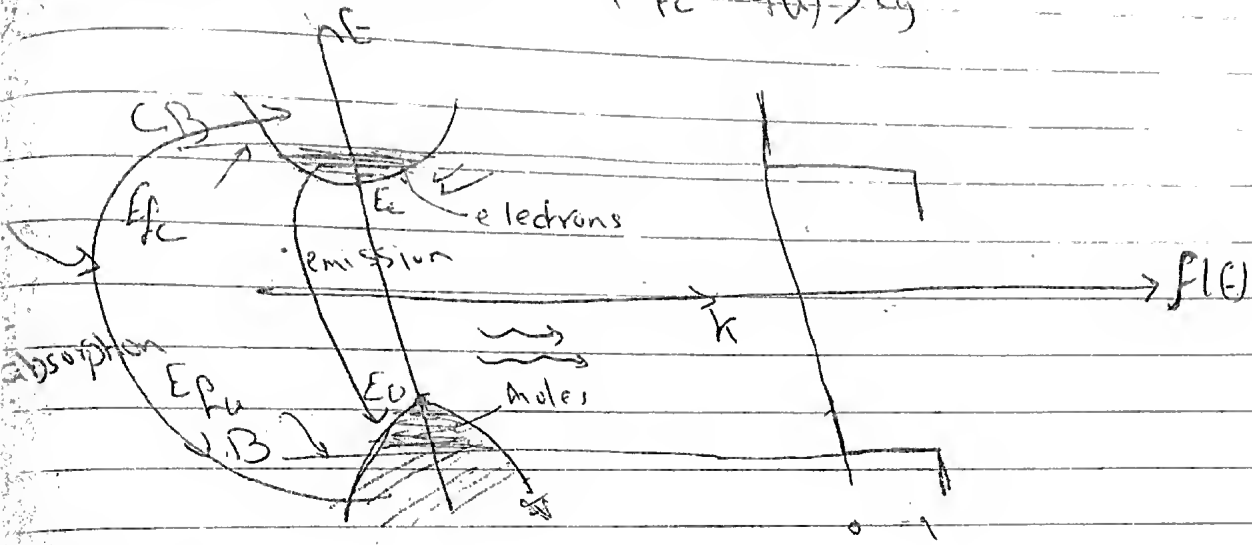
$$\delta = -ve$$

attenuator



Quasi equilibrium

$$(E_F - E_{FV}) > E_g$$



$$f(E_c) = 1$$

$$f(E_v) = 0$$

$$f_c(E_c) - f_v(E_v) = 1$$

$$\delta = +ve$$

Amplifier

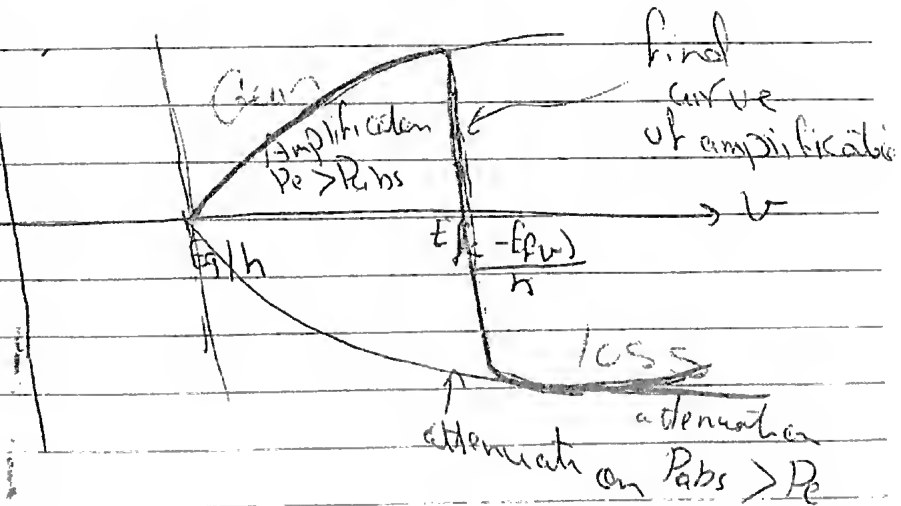
emission process will also be photon δ ~~be~~ δ

$E_{Fc} - E_{Fv}$ is greater than E_g is

absorption process will also be photon δ ~~be~~ δ

$E_{Fc} - E_{Fv}$ is not greater than E_g is

δ



ex:- $E_g = 1 \text{ eV}$

$E_c - E_v \approx 1.2 \text{ eV}$

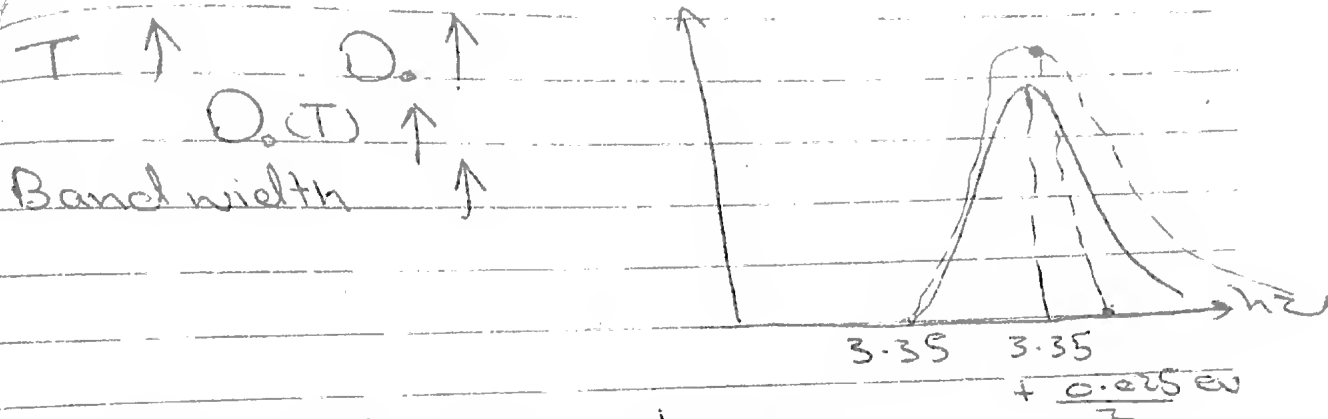
$$\frac{E_g}{h} = \frac{1 \times 1.6 \times 10^{-19}}{6.6 \times 10^{-34}} \approx 0.25 \times 10^{15} \text{ Hz} = \underline{\underline{250 \text{ THz}}}$$

$$\frac{E_c - E_v}{h} = \frac{1.2 \times 1.6 \times 10^{-19}}{6.6 \times 10^{-34}} =$$

$$BW \approx \frac{0.2 \times 1.6 \times 10^{-19}}{6.6 \times 10^{-34}} \quad \ll$$

GaN

$$E_g = 3.35 \text{ eV}$$



جزيء (فعل) لا يمكنه

Semiconduct Direct mat

Bumping Forward Bias

X
Ces
عربي
الذي

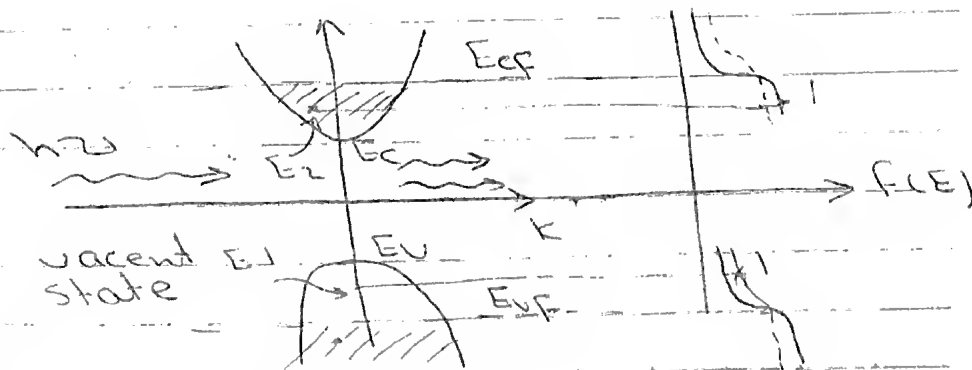
lec (15)

الذي

$$\gamma = \frac{(c/n)^2 (2m)^{3/2} (h\nu - E_g)^{1/2}}{2T_r (h\nu)^2}$$

$$X (f_c(E_2) - f_v(E_1))$$

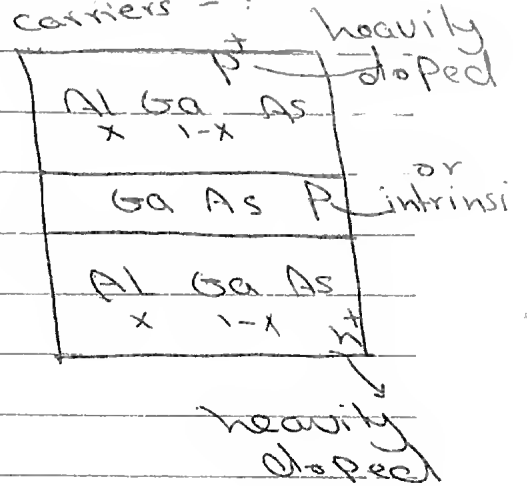
$$\text{at } T = 0 \text{ K } f_c(E_2) - f_v(E_1) = 1$$



II

double heterostructure

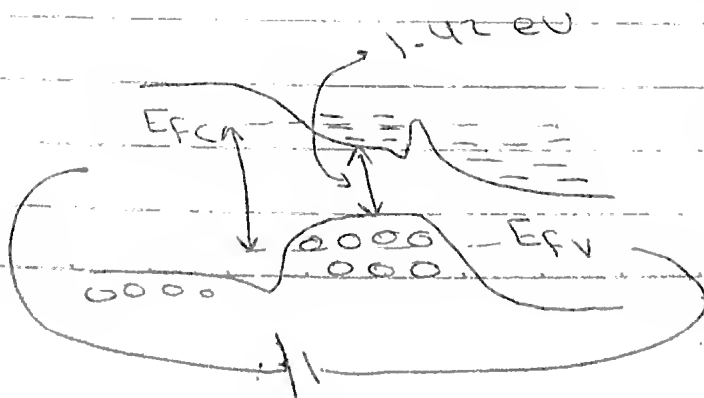
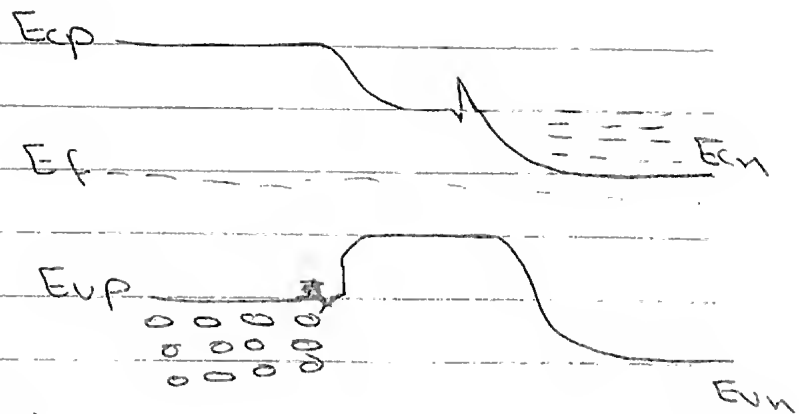
majority carriers = holes



minority
carries
electrons

$$E_g = 1.42 \text{ eV}$$

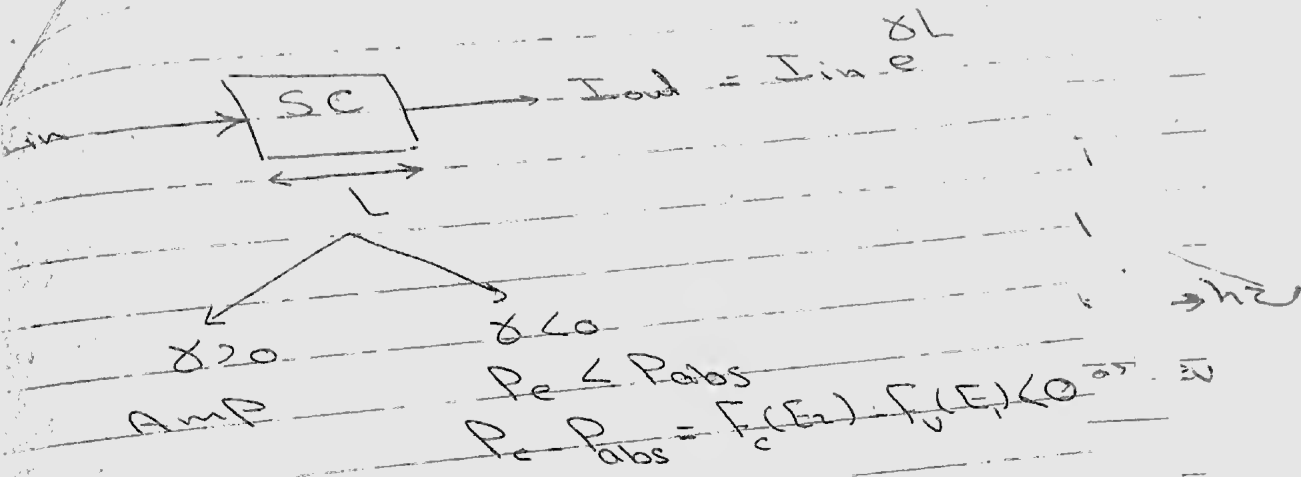
Steady state



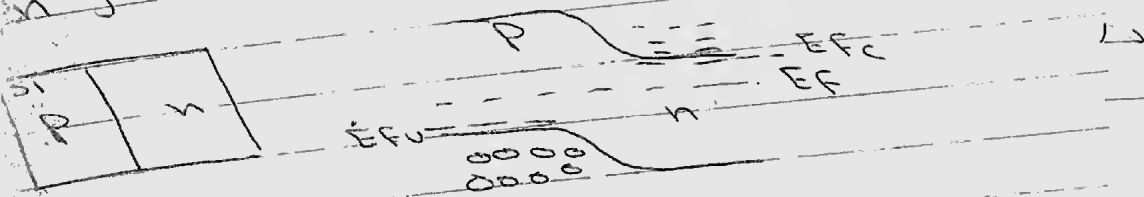
في حالة الفوسل
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31

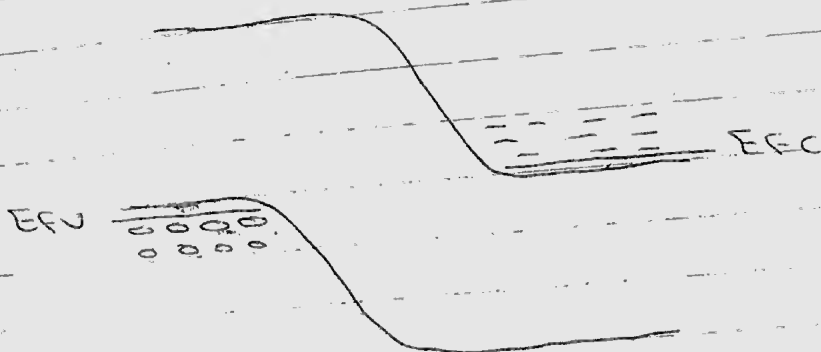
Attenuation



n junction



input \downarrow ooooo \uparrow --- FB closed
R.B. closed output



Absorp Spectrum

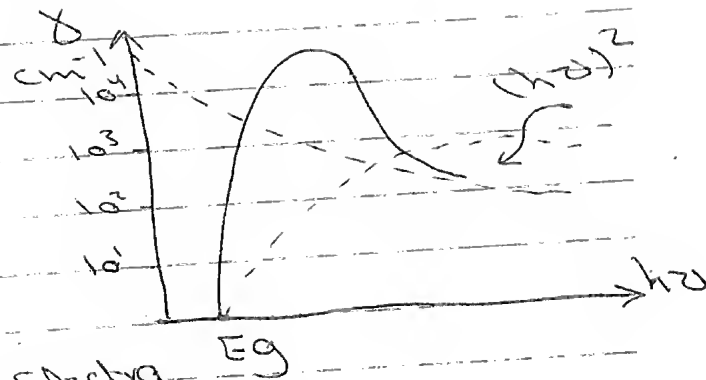
$$\delta = -\alpha_{\text{abs}}$$

arell no celsil

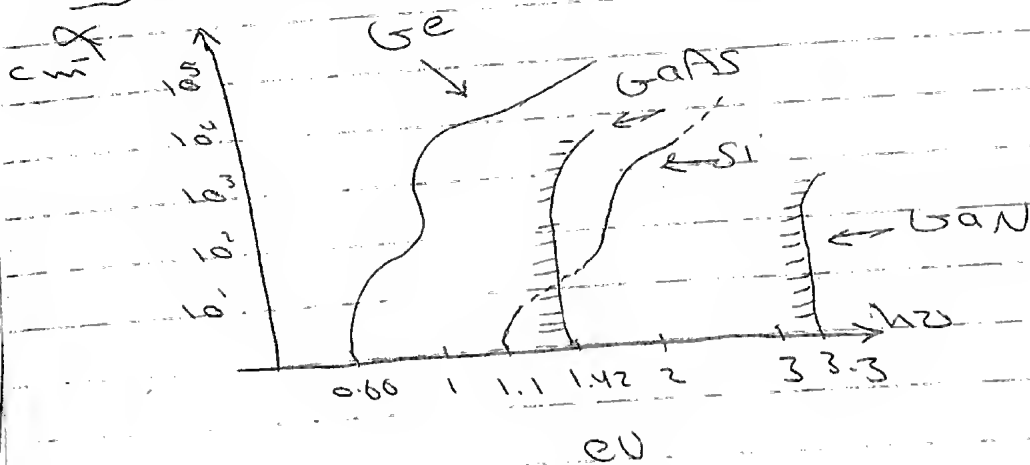
all well

$$(h\nu - E_g)^{1/2}$$

$$\alpha_{\text{abs}} = \frac{(c/n)^2 (2\pi\nu)^{3/2}}{2Z_r (h\nu)^2}$$



Typical Absorption Spectra



Comments on curve

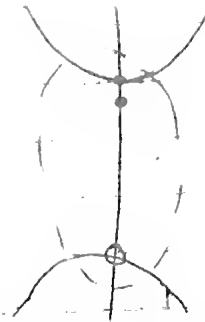
* Any material either Direct or Indirect absorp

* Absorption increases with freq

→ curves consider indirect band gap

E_g - Binding energy
(10 meV)

All Energy states
expanded



attraction
Coulomb's force

Excited electron hole
pair

report about (4) Nanostructure mat

lec (16)

المواد

Photo conductors

Device that its conductivity changes
with the light incidence

Photodiode Photoresistor Phototransi Solar cell

↓

Pn PIN APD

General ck's

1. Quantum efficiency η
2. Responsivity R
3. Response time
4. Noise Power

(17)

created carrier flux $\frac{I_{ph}}{e}$

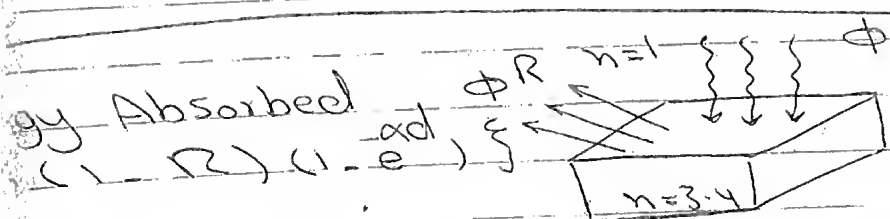
incident photon flux $\frac{P_{opt}}{h\nu}$

power

$$\frac{I_{ph}}{P_{opt}} \left(\frac{h\nu}{e} \right) \rightarrow \left(\frac{h}{e} \right) \left(\frac{c}{\lambda} \right) = \frac{1.24}{\lambda (\mu m)}$$

$\downarrow R (A)$

$$R = \frac{1.24}{\lambda (\mu m)} \quad R = \frac{1.24}{\lambda (\mu m)}$$



absorption coefficient material

$$\eta = (1-R)(1-e^{-\alpha d}) \quad \left(\frac{\eta}{\alpha} \right) \quad 1 \geq \eta \geq 0$$

how to maximize η ?

R (reflection) \ll
 coating In_2O_3
 Indium tin oxide In_2O_3
 thickness of coating mat function of
 incident wavelength

Designed PD is tuned at specific wavelength

② $\alpha d \ll 1$

$\alpha d \gg 1$

(thickness of PD) $\uparrow \uparrow$

$\propto \uparrow \uparrow$ (atten const)

المادة $\alpha \ll 1$ $d \gg 1$ $\alpha d \gg 1$

③ } material ~~functions~~ fabrication \downarrow

\leftarrow less dangling bonds \leftarrow less defects

less trap states \rightarrow high performance

② R
المادة $\alpha \ll 1$
جاء بؤرة ال

①

R

InGaAs

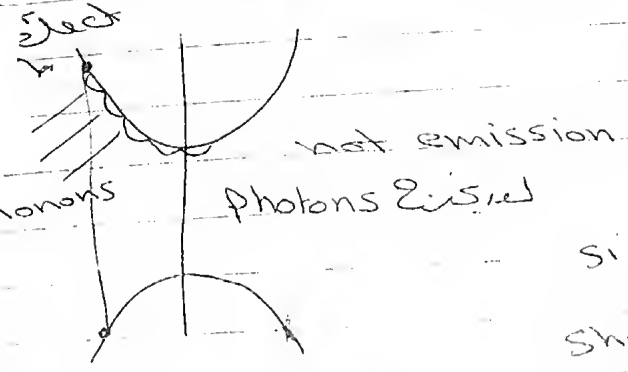
Si

Short wavelength

Long wavelength

1100 nm position

~ 1.5
min $E_g \equiv \text{MAX } \lambda$



thermionization
المادة $\alpha \ll 1$
R curve, abs curve

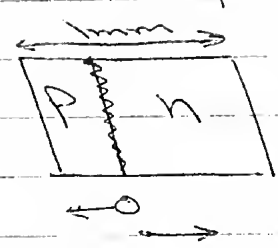
③

InGaAs	μ_e 14000	μ_h 400
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$\mu_e > \mu_h$ \therefore $t_{se} < t_{sh}$
 To min time response

① dimension of n & p layers in PD should be adjusted as shown in below to achieve compromise speed for ie, t_{sh}

② Choose material with high mobility

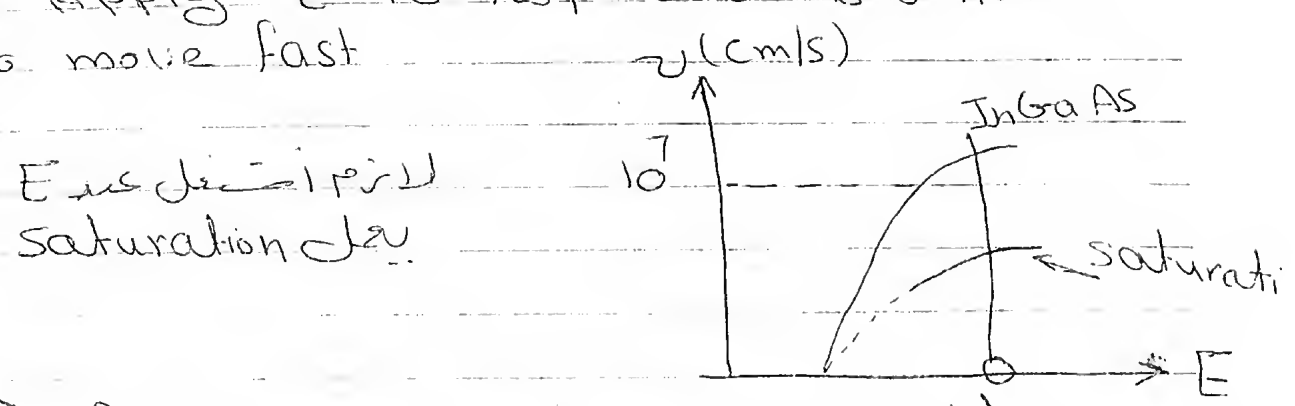


ex):

$$t_{se} = \frac{1\text{mm}}{\mu_e} \quad \mu_e = 10^7 \text{ cm/s}$$

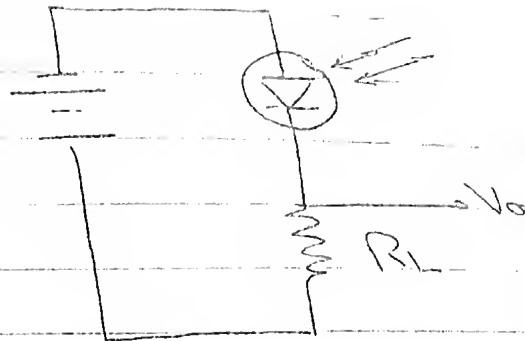
$$t_{se} \approx 10^{-8} \text{ s} \quad \mu \uparrow \quad t_s \downarrow$$

③ Apply E to help electrons & holes to move fast



② Recombination time in circuit

$$\text{response} \uparrow \quad \text{recom } t \downarrow \quad R_L, C \downarrow$$

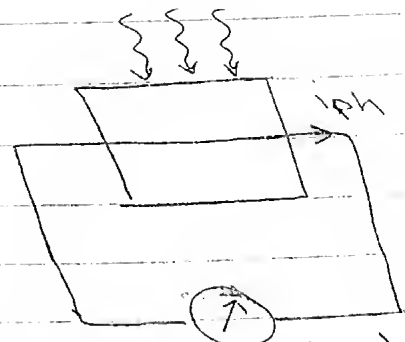


Give reason to use InGaAs

- ① R. curve
- ② High speed \rightarrow low time response

Noise power

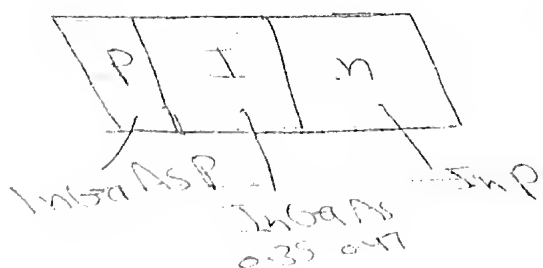
dark current generated
reverse circuit without
incident light



dark current generated

Si	~ 1 nA	dark current
InGaAs	~ 10 nA	Sensing
Ge	~ 100 nA	noise power

Common PD Design is PIN



P-type (+ve)
n-type (-ve)
intrinsic mat

(3)